



Problem of the Week Problem C and Solution Drying Fruit

Problem

Fruit can be preserved through drying to remove excess moisture.

The water content of a certain fruit, by mass, is 70%. Therefore, 30% of the fruit, by mass, is other material.

When left in the sun to dry, the fruit loses 80% of its water content, and the amount of other material remains the same.

Rounded to the nearest tenth, what percent of the dried fruit is water?

Solution

Solution 1

Let's consider a piece of fruit that originally weighs 100 g. Since 70% of the mass is water, that means that 70 g is water and 30 g is other material.

When left in the sun to dry, the fruit loses 80% of its water mass. So it loses 80% of $70 \text{ g} = 0.8 \times 70 = 56 \text{ g}$ of water, and 70 - 56 = 14 g of water remains.

The dried fruit still contains 30 g of other material. Therefore, the dried fruit consists of 14 g of water and 30 g other material, for a total of 44 g.

Therefore, the dried fruit is $\frac{14}{14+30} \times 100\% = \frac{14}{44} \times 100\% \approx 31.8\%$ water.

Solution 2

Suppose the fruit originally weighs x g. Since 70% of the mass is water, that means that 70% of $x = 0.7 \times x = 0.7x$ g is water and 30% of x = 0.3x g is other material.

When left in the sun to dry, the fruit loses 80% of its water mass. So it loses 80% of $0.7x = 0.8 \times 0.7x = 0.56x$ g of water, and therefore 0.7x - 0.56x = 0.14x g of water remains.

The dried fruit still contains 0.3x g of other material. Therefore, the dried fruit consists of 0.14x g of water and 0.3x g of other material, for a total of 0.44x g.

Therefore, the dried fruit is $\frac{0.14x}{0.14x + 0.30x} \times 100\% = \frac{0.14x}{0.44x} \times 100\% \approx 31.8\%$ water.