# Problem of the Week Problem B and Solution 

## Server Satisfaction

## Problem

You've just enjoyed a delicious meal at a restaurant with your friend. The cost of the meal before tax and tip was $\$ 35.10$.
(a) Suppose the tax is $15 \%$ of the total cost. Estimate the dollar amount of tax using a mental math strategy. Then calculate the actual dollar amount of tax, and total cost including tax.
(b) If you want to tip the server an additional $20 \%$ after tax, how much would you pay in total?
(c) How much change would you receive if you paid with a $\$ 100$ bill?

Extension: Suppose you are a server. In general, when would you rather receive a $\$ 20$ tip instead of $20 \%$ of your bill? Justify your thinking.


## Solution

(a) To estimate the dollar amount of tax, we could first round the total cost to $\$ 35$. Then we could think of $15 \%$ as $10 \%+5 \%$. Since $10 \%$ of $\$ 35$ is $\$ 3.50$, and half of that is $\$ 1.75$, we can estimate that the dollar amount of tax is $\$ 3.50+\$ 1.75=\$ 5.25$.
The actual dollar amount of tax is $\$ 35.10 \times 0.15=\$ 5.265$, which rounds to $\$ 5.27$. Thus, the total cost including tax is $\$ 35.10+\$ 5.27=\$ 40.37$.
(b) If you want to tip the server an additional $20 \%$, then we need to calculate $20 \%$ of $\$ 40.37$. We know that $10 \%$ of $\$ 40.37$ is $\$ 4.037$. We then double that to get $20 \%$, which is $\$ 8.074$. Rounded to the nearest cent, this is $\$ 8.07$. Finally, adding that to the total cost including tax gives $\$ 40.37+\$ 8.07=\$ 48.44$.
(c) If you paid with a $\$ 100$ bill, your change would be $\$ 100-\$ 48.44=\$ 51.56$.

Extension: When $20 \%$ of the total cost including tax is less than $\$ 20$, then a $\$ 20$ tip would likely be preferred. When $20 \%$ of the total cost including tax is greater than $\$ 20$, then a tip of $20 \%$ would likely be preferred.

