Problem of the Week Problem E A Lot of Zeros

For a positive integer n, the product of the integers from 1 to n can be written in abbreviated form as n!, which we read as "n factorial". So,

$$n! = n \times (n-1) \times (n-2) \times \dots \times 3 \times 2 \times 1$$

For example,

 $6! = 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 720$, and $11! = 11 \times 10 \times 9 \times \cdots \times 3 \times 2 \times 1 = 39\,916\,800.$

Note that 6! ends in one zero and 11! ends in two zeros.

Determine the smallest positive integer n such that n! ends in exactly 1000 zeros.

