

An activity of The Centre for Education in Mathematics and Computing, University of Waterloo, Waterloo, Ontario

Pascal Contest (Grade 9)

Wednesday, February 23, 2000

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Time: 1 hour

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Calculators are permitted, providing they are non-programmable and without graphic displays.

Instructions

- 1. Do not open the contest booklet until you are told to do so.
- 2. You may use rulers, compasses and paper for rough work.
- 3. Be sure that you understand the coding system for your response form. If you are not sure, ask your teacher to clarify it. All coding must be done with a pencil, preferably HB. Fill in circles completely.
- 4. On your response form, print your school name, city/town, and province in the box in the upper right corner.
- 5. Be certain that you code your name, age, sex, grade, and the contest you are writing on the response form. Only those who do so can be counted as official contestants.
- 6. This is a multiple-choice test. Each question is followed by five possible answers marked **A**, **B**, **C**, **D**, and **E**. Only one of these is correct. When you have decided on your choice, fill in the appropriate circles on the response form.
- 7. Scoring: Each correct answer is worth 5 in Part A, 6 in Part B, and 8 in Part C.

There is no penalty for an incorrect answer.

Each unanswered question is worth 2, to a maximum of 20.

- 8. Diagrams are *not* drawn to scale. They are intended as aids only.
- 9. When your supervisor instructs you to begin, you will have sixty minutes of working time.

Each unanswered question is worth 2 credits, to a maximum of 20 credits.

Part A: Each correct answer is worth 5.

The value of $5^2 + 2(5-2)$ is

- (**A**) 16
- **(B)** 19
- **(C)** 31
- **(D)** 36

(E) 81

The sum of 29 + 12 + 23 is

- **(A)** 32^2 **(B)** 2^6
- (C) 3^4
- **(D)** 1⁶⁴

(E) 64^0

If x = 4 and y = -3, then the value of $\frac{x - 2y}{x + y}$ is

- **(A)** $-\frac{1}{2}$ **(B)** -2 **(C)** $\frac{10}{7}$ **(D)** $-\frac{2}{7}$

(E) 10

If the following sequence of five arrows repeats itself continuously, what arrow would be in the 48th position?



5. If $y = 6 + \frac{1}{6}$, then $\frac{1}{y}$ is

- (A) $\frac{6}{37}$ (B) $\frac{37}{6}$ (C) $\frac{6}{7}$

(E) 1

6. If $\frac{2}{3}$, $\frac{23}{30}$, $\frac{9}{10}$, $\frac{11}{15}$, and $\frac{4}{5}$ are written from smallest to largest then the middle fraction will be

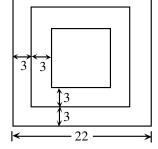
- (**A**) $\frac{23}{30}$
- **(B)** $\frac{4}{5}$
- (C) $\frac{2}{3}$
- **(D)** $\frac{9}{10}$

(E) $\frac{11}{15}$

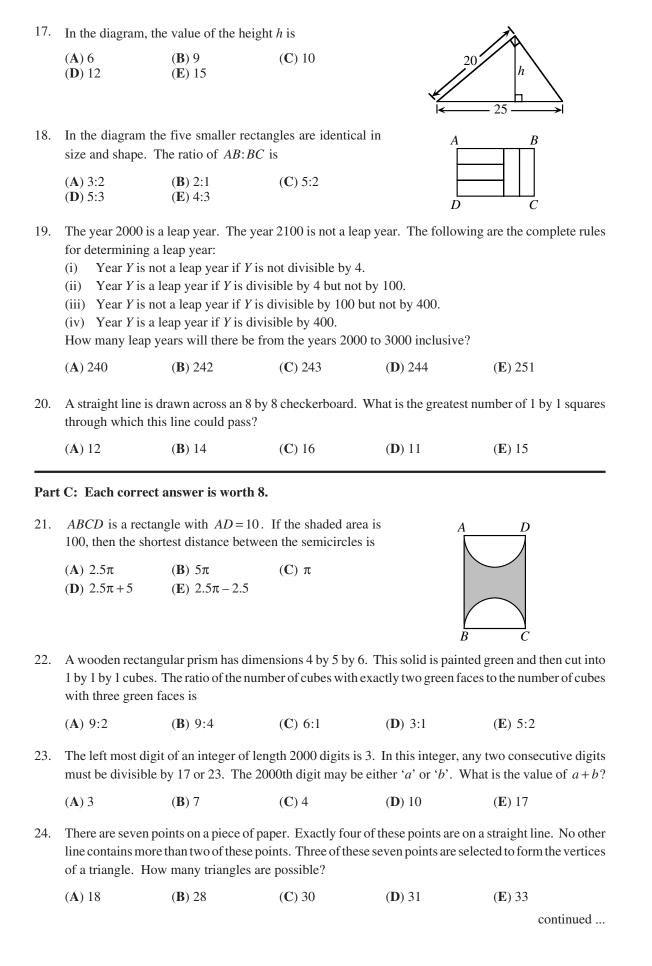
Three squares with the same centre and corresponding parallel sides are drawn. The distance between the sides of successive squares is 3 and the side length of the largest square is 22, as shown. What is the perimeter of the smallest square?

- (A) 40
- **(B)** 100
- (C) 10

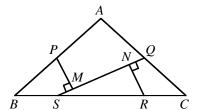
- (**D**) 64
- (E) 20



| 8. | In the diagram, the value of y is r° | | | | | |
|------|--|-------------------------------------|---|--|--------------------------------------|--|
| 0. | (A) 30 (D) 60 | (B) 20 (E) 40 | (C) 80 | 60° | $2x^{\circ}$ x° y° | |
| 9. | The ages of three contestants in the Pascal Contest are 14 years, 9 months; 15 years, 1 month; and 14 years, 8 months. Their average (mean) age is | | | | | |
| | (A) 14 years, 8 months (D) 14 years, 11 months | | (B) 14 years, 9 i (E) 15 years | (B) 14 years, 9 months (E) 15 years (C) 14 years, 10 months | | |
| 10. | The number of integers between $-\sqrt{8}$ and $\sqrt{32}$ is | | | | | |
| | (A) 5 | (B) 6 | (C) 7 | (D) 8 | (E) 19 | |
| Part | B: Each corre | ect answer is wort | h 6. | | | |
| 11. | A store had a sale on T-shirts. For every two T-shirts purchased at the regular price, a third T-shirt was bought for \$1.00. Twelve T-shirts were bought for \$120.00. What was the regular price for one T-shirt? | | | | | |
| | (A) \$10.00 | (B) \$13.50 | (C) \$14.00 | (D) \$14.50 | (E) \$15.00 | |
| 12. | In the diagram, every number beginning at 30 equals twice the sum of the two numbers to its immediate left. The value of c is $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | | | |
| | (A) 50 (D) 100 | (B) 70 (E) 200 | (C) 80 | | | |
| 13. | In the expression $\frac{a}{b} + \frac{c}{d} + \frac{e}{f}$ each letter is replaced by a different digit from 1, 2, 3, 4, 5, and 6. What is the largest possible value of this expression? | | | | | |
| | | (B) $9\frac{5}{6}$ | • | (D) $9\frac{2}{3}$ | (E) $10\frac{1}{3}$ | |
| | (\mathbf{A}) $6\frac{1}{3}$ | (B) $9\frac{1}{6}$ | (C) $9\frac{1}{3}$ | (D) $9\frac{1}{3}$ | (E) $10\frac{1}{3}$ | |
| 14. | The numbers 6, 14, x , 17, 9, y , 10 have a mean of 13. What is the value of $x + y$? | | | | | |
| | (A) 20 | (B) 21 | (C) 23 | (D) 25 | (E) 35 | |
| 15. | The digits 1, 1, 2, 2, 3, and 3 are arranged to form an odd six digit integer. The 1's are separated by one digit, the 2's by two digits, and the 3's by three digits. What are the last three digits of this integer? | | | | | |
| | (A) 3 1 2 | (B) 1 2 3 | (C) 1 3 1 | (D) 1 2 1 | (E) 2 1 3 | |
| 16. | The area of square $ABCD$ is 64. The midpoints of its sides are joined to form the square $EFGH$. The midpoints of its sides are J , K , L , and M . The area of the shaded region is | | | | | |
| | (A) 32 (D) 28 | (B) 24 (E) 16 | (C) 20 | E M | H C | |



25. $\triangle ABC$ is an isosceles triangle in which AB = AC = 10 and BC = 12. The points S and R are on BC such that BS:SR:RC = 1:2:1. The midpoints of AB and AC are P and Q respectively. Perpendiculars are drawn from P and R to SQ meeting at M and N respectively. The length of MN is



- **(A)** $\frac{9}{\sqrt{13}}$ **(B)** $\frac{10}{\sqrt{13}}$ **(C)** $\frac{11}{\sqrt{13}}$
- **(D)** $\frac{12}{\sqrt{13}}$ **(E)** $\frac{5}{2}$