2015 Beaver Computing Challenge (Grade 9 & 10)

Questions
Part A
Five beavers join an online social network resulting in the following activity:

- Ari follows Bob
- Ari follows Dmitri
- Bob follows Chio
- Bob follows Dmitri
- Chio follows Ari
- Chio follows Bob
- Dmitri follows Ehab
- Ehab follows Bob

Then, we track how popular various beavers are. We give $n$ popularity points to beaver $Y$ if beaver $X$ follows beaver $Y$ and there are $n$ beavers that follow beaver $X$. We compute beaver $Y$’s total popularity points by adding up all such points from all the beavers that follow beaver $Y$. For example, Bob has 3 popularity points.

**Question**

Which beaver has the most popularity points?

(A) Ari
(B) Bob
(C) Chio
(D) Dmitri
Tommy Beaver was inspired by the picture of an animal made from nuts (shown to the right), and created 4 animals by himself using chestnuts, strings and glue (shown below):

<table>
<thead>
<tr>
<th>Starfish</th>
<th>Dog</th>
<th>Sea lion</th>
<th>Giraffe</th>
</tr>
</thead>
</table>

His sister plays with these animals by moving the chestnuts around without breaking any connections. This makes it hard to recognize which shapes correspond to which animals.

Which animal was the following shape before Tommy Beaver’s sister played with it?

(A) Starfish
(B) Dog
(C) Sea lion
(D) Giraffe
Allison Beaver has a pile of 10 trees. Beatrice Beaver has only 1 tree.

Allison Beaver and Beatrice Beaver start chewing trees in a forest at exactly the same time. They add every tree they chew down to their own pile of trees.

Alison Beaver chews down one tree per hour.

Beatrice Beaver chews down trees at a different rate. In the first hour, she will chew down one tree. In the second hour, she will chew down two trees. In the third hour, she will chew down three trees, and so on.

After how many hours will Beatrice first have at least as many trees as Allison?

(A) 4
(B) 5
(C) 6
(D) 7
Beavers want to encode numbers for keeping track of how many trees they have chewed down. Therefore they developed the Quick-Beaver-Code (QB-Code). This is a graphical code consisting of nine $1 \times 1$ squares arranged into a $3 \times 3$ square. Every square has a certain value. The squares are filled line by line from the bottom to the top, from right to left. The next square has double the value of the square before. In the example, you see the values of the first five squares.

To encode a number, the beavers darken some squares. The number encoded is the sum of the values of the dark squares.

For example, the number encoded in this QB-Code is 17:

![QB-Code Example](image)

Which of the following encodes the largest number?

(A) 
(B) 
(C) 
(D)
Beavers have created a nifty irrigation system for their fields. The water flows from a lake at the top of the hill all the way down to the fields numbered 1 to 6 at the bottom. Along the water canals, the beavers have installed four water gates A to D, where the water can only flow either to the left (←) or to the right(→). An example showing how these may be set to have the water flow to fields 1, 2, 5 and 6 is shown below.

What is the correct configuration for the water gates to irrigate only fields 2, 4, 5 and 6?

(A) A: ← B: ← C: → D: ←
(B) A: → B: ← C: ← D: →
(C) A: → B: ← C: → D: ←
(D) A: ← B: → C: → D: →
Part B
Collecting Pollen

Beever the bee flies to a field of flowers to collect pollen. On each flight, he visits only one flower and can collect up to 10 mg of pollen. He may return to the same flower more than once.

The initial amount of pollen in each flower (in mg) is shown below.

What is the maximum total amount of pollen that Beever can collect in 20 flights?

(A) 179 mg
(B) 195 mg
(C) 196 mg
(D) 200 mg
There are seven dens in a pond just off a shore as shown below. Dotted lines show where bridges can be built. The numbers show how many trees are needed to build each possible bridge. A beaver needs to decide which bridges to build so that any den can be reached from the shore without swimming.

Story

What is the fewest number of trees needed to build the bridges?

(A) 12
(B) 13
(C) 17
(D) 18
Robotic Car

Story

Beavers have developed a robotic car. It has sensors that detect intersections. It produces the sounds shown below, when it is possible to turn left, right or both directions. The robotic car can go straight through an intersection (when possible), turn right (when possible) or turn left (when possible). The robotic car cannot make U-turns and cannot reverse.

It automatically stops when it senses an obstacle in front of it.

Question

The car drives around the map shown below, starting at the indicated position. As it drives around the map, it produces the sounds Huiii Ding Huiii Dong, in that order.

At which location does the car stop?

(A) Location A
(B) Location B
(C) Location C
(D) Location D
A beaver moves in strange ways. He starts at the middle position, as shown below. He will make five moves, alternating between right (R) and left (L): he first moves right, then left, then right, then left, and finally, right.

On each move, he can jump 1, 2, 3, 4 or 5 positions from his current position. He picks each distance exactly once. For example, he can move R by 2, L by 1, R by 5, L by 4 and R by 3, ending at $2 - 1 + 5 - 4 + 3 = 5$ positions to the right from where he started.

For your convenience, every second position is shaded.

Out of the four positions marked by a letter, there is one that he cannot end up on. Which one?

(A) Position marked A.
(B) Position marked B.
(C) Position marked C.
(D) Position marked D.
Three kinds of buttons control a robot:

<table>
<thead>
<tr>
<th>Button</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>↑</td>
<td>robot turns left</td>
</tr>
<tr>
<td>↓</td>
<td>robot turns right</td>
</tr>
<tr>
<td>X</td>
<td>robot moves $X$ units in the direction it is facing</td>
</tr>
</tbody>
</table>

The robot starts at the blue star facing east. John presses the seven buttons shown (from left to right) to try and move the robot to the red diamond. Unfortunately, he presses two extra buttons by mistake.

Which two button presses should be removed so that the robot ends at the correct location?

(A) the 1st and the 2nd
(B) the 1st and the 4th
(C) the 3rd and the 4th
(D) the 2nd and the 6th
Part C
A king loves long travels in his coach, so he orders his coachman to never go straight when reaching a new road. That is, the coachman must turn either right or left if he comes to any intersection. This applies even for intersections with three roads.

On the image to the right you see a road map of the country. Roads are shown as red vertical or horizontal lines. All roads connecting two adjacent intersections are 1 km long.

The king needs to go from the bottom left corner, marked Start, to the top right corner, marked Finish. The coachman however, wants to get to the destination as quickly as possible.

Find a shortest path for the coachmen from start to the finish that does not break the rule that the coach can never go straight. What length does it have?

(A) 11 km
(B) 13 km
(C) 15 km
(D) It is not possible to get to the destination without breaking the rule.
Beaver John plans to go to the beach tomorrow, but he will go only if there will be at least three sunny hours between 13:00 and 19:00 (which is 24-hour time for 1:00pm and 7:00pm). He has a file containing the hourly weather forecasts, made up of 24 lines corresponding to each hour of the day, from 00:00-01:00 to 23:00-24:00; each line contains one of the words sunny, cloudy, rainy, or snowy. He can use the following commands:

- **ONLY** $w$ selects only the lines containing the word $w$
- **FIRST** $n$ selects the first $n$ lines (or all the lines if there are fewer than $n$ lines)
- **LAST** $m$ selects the last $m$ lines (or all the lines if there are fewer than $m$ lines)
- **COUNT** counts the number of lines in its input

Using | as a separator, John can combine these commands in sequence as he likes: the output of any command in the sequence will be the input of the following command. For example, the sequence

```
A | B | C
```

where A, B and C are commands from the list, indicates that the output of A is used as the input for B; the output of B is then used as the input for C. The input to the first command is always the content of the file of forecasts.

**Question**

How can John arrange the previous commands in order to decide whether or not he will go to the beach?

(A) **FIRST** 19 | **LAST** 6 | **ONLY** sunny | **COUNT**

(B) **ONLY** sunny | **FIRST** 19 | **LAST** 6 | **COUNT**

(C) **FIRST** 20 | **LAST** 7 | **ONLY** sunny | **COUNT**

(D) **LAST** 20 | **FIRST** 6 | **ONLY** sunny | **COUNT**
Two beavers live in lodges separated by a large forest. They decide to send messages to each other by shooting fireworks into the sky above the trees. Each message is a sequence of words, but the beavers only know five words. They shoot two types of fireworks one after the other according to the following code:

<table>
<thead>
<tr>
<th>Word</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>log</td>
<td><img src="image1" alt="Fireworks1" /></td>
</tr>
<tr>
<td>tree</td>
<td><img src="image3" alt="Fireworks3" /></td>
</tr>
<tr>
<td>rock</td>
<td><img src="image6" alt="Fireworks6" /></td>
</tr>
<tr>
<td>den</td>
<td><img src="image9" alt="Fireworks9" /></td>
</tr>
<tr>
<td>food</td>
<td><img src="image11" alt="Fireworks11" /></td>
</tr>
</tbody>
</table>

For example, to send the (strange) message “food, log, food”, a beaver would shoot:

How many different meanings does the following sequence of fireworks have?

(A) 1  
(B) 2  
(C) 3  
(D) 4
Every Friday, six spies share all the information they have gathered that week. A spy can never be seen with more than one other spy at the same time. They have to conduct several rounds of meetings where they meet up in pairs and share all information they have at that point. The group of 6 spies needs only three rounds to distribute all information. Before the meetings, each spy holds a single piece of information. (spy 1 knows “a”, spy 2 knows “b”, etc.). In the first round, spies 1 and 2 meet and share information so now both know “ab”. The diagram shows the initial information as well as the three rounds of meetings, with lines indicating which spies meet in each round. It also shows which pieces of information they all have. After three rounds all information has been distributed.

After an international incident one spy has stopped attending the meetings. What is the minimum number of rounds needed for the five remaining spies to share all information?

(A) 2
(B) 3
(C) 4
(D) 5
Beaver the Alchemist can convert objects into other objects. He can convert:

- two clovers into a coin;
- a coin and two clovers into a ruby;
- a ruby and a clover into a crown;
- a coin, a ruby, and a crown into a kitten.

After objects have been converted to another object, they disappear.

Initially Beaver the Alchemist has lots of clovers, but no coins, rubies, crowns or kittens.

**Question**

How many clovers does Beaver the Alchemist need to create one kitten?

(A) 5
(B) 10
(C) 11
(D) 12