Problem

Hakim has received \$30.00 as a birthday gift and wants to spend it on treating three friends and himself to lunch. The menu includes:



Main		\mathbf{Sides}		\mathbf{Drinks}	
Hamburger	\$4.00	French Fries	\$2.00	Regular	\$1.25
Cheeseburger	\$4.50	Onion Rings	\$2.50	Large	\$1.75
Veggie Burger	\$3.50				

- a) If each of the four boys orders 1 main, 1 side and 1 drink, in how many different ways could the boys select their lunch items?
- b) Suppose each boy orders the same three items. Which combinations can Hakim afford to pay for with his birthday money?

Hints

Hint 1 - Make a tree to see how many combinations exist.

Solution

- a) Represent the different food choices as follows:
 - H hamburger, C cheeseburger, V veggie burger,
 - F french fries, O onion rings,
 - R regular drink, L large drink.

Creating the tree as shown at right, we see that there is a total of 12 different ways the boys could select their lunch items.

- b) If each boy selects the same three items, each lunch will cost the same. Since Hakim has only \$30, each lunch can cost at most $$30 \div 4 = 7.50 . Assigning costs to each of the choices reveals that the only combinations Hakim could afford are:
 - hamburger + french frieds + regular drink (\$7.25);
 - veggie burger + french frieds + regular drink (\$6.75);
 - veggie burger + french frieds + large drink (\$7.25); or
 - veggie burger + onion rings + regular drink (\$7.25).

